# PAL-EUV Beam Dynamics study 

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Outline

* PAL-EUV booster
- Current design
- Alternative design (preliminary)
- Comparison


## * PAL-EUV storage ring

- Current design
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* Summary


## Motivation

- PAL-EUV is a compact size accelerator complex consists of gun, 20 MeV linac, 22.2 m booster and $36.0 \mathrm{~m}-400 \mathrm{MeV}$ storage ring
- Although it has compact size, its nonlinear property is as strong as a typical 4GSR machine (e.g. small dynamic aperture, small momentum aperture)
- This study investigates dynamic property of current PAL-EUV design and explores alternative designs providing better nonlinearity and robustness
- Design of compact size and low energy storage ring is somewhat delicate due to
- Long damping time (damping time $\propto \frac{1}{E^{3}}$ )
- Short Touschek lifetime (Touschek lifetime $\propto E^{3}$ )
- Strong dipole edge-focusing effect
- Dense arrangement of magnets and possible strong cross-talk


## ※PAL-EUV booster

- Current design
- Alternative design (preliminary)
- Comparison


## PAL-EUV booster (current design)



| Parameters | Value |
| :---: | :---: |
| Energy (MeV) | 20-400 |
| Circumference (m) | 22.20 |
| Equilibrium emittance ( nm ) <br> @ 400 MeV | 1.75 |
| Tunes (H,V) | 4.84 / 3.66 |
| Natural chromaticity ( $\mathrm{H}, \mathrm{V}$ ) | -11.2/-15.7 |
| Chromaticity (corrected) $(\mathrm{H}, \mathrm{~V})$ | 1, 1 |
| Hor. Damping partition | 2.0459 |
| Momentum compaction | $2.798 \times 10^{-2}$ |
| Energy spread ( $\sigma_{\delta}$ ) <br> @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{gathered} 0.019 \times 10^{-3} / \\ 0.389 \times 10^{-3} \end{gathered}$ |
| Energy loss per turn (keV) <br> @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{gathered} 0.0 / \\ 1.4 \end{gathered}$ |
| Main RF voltage (keV) | 70 |
| Damping time ( $\mathrm{H} / \mathrm{V} / \mathrm{Z}$ ) (ms) <br> @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{aligned} & 166066 / 339759 / 356113 \\ & 20.76 / 42.47 / 44.51 \end{aligned}$ |

## PAL-EUV booster alternative design (preliminary)



| Parameters | Value |
| :---: | :---: |
| Energy (MeV) | 20-400 |
| Circumference (m) | 34.680 |
| Equilibrium emittance ( nm ) <br> @ 400 MeV | 30.96 |
| Tunes (H,V) | 2.42, 1.38 |
| Natural chromaticity ( $\mathrm{H}, \mathrm{V}$ ) | -2.1, -1.8 |
| Chromaticity (corrected) $(\mathrm{H}, \mathrm{~V})$ | 1, 1 |
| Hor. Damping partition | 1.648 |
| Momentum compaction | 0.1408 |
| Energy spread ( $\sigma_{\delta}$ ) <br> @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{gathered} 0.014 \times 10^{-3} / \\ 0.285 \times 10^{-3} \end{gathered}$ |
| Energy loss per turn (keV) <br> @20 MeV / 400 MeV | $\begin{gathered} 0.0 / \\ 1.5 \end{gathered}$ |
| Main RF voltage (keV) | 70 |
| Damping time ( $\mathrm{H} / \mathrm{V} / \mathrm{Z}$ ) ( ms ) <br> @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{aligned} & 450494 / 499538 / 264147 \\ & 56.31 / 62.44 / 33.02 \end{aligned}$ |

## Comparison on lattice parameters and magnets

Lattice parameters

| Parameters | Current design | Alternative design |
| :---: | :---: | :---: |
| Energy (MeV) | 20-400 | 20-400 |
| Circumference (m) | 22.20 | 34.680 |
| Equilibrium emittance ( nm ) <br> @ 400 MeV | 1.75 | 30.96 |
| Tunes ( $\mathrm{H}, \mathrm{V}$ ) | 4.84 / 3.66 | 2.42, 1.38 |
| Natural chromaticity ( $\mathrm{H}, \mathrm{V}$ ) | -11.2/-15.7 | -2.1, -1.8 |
| Chromaticity (corrected) $(\mathrm{H}, \mathrm{~V})$ | 1, 1 | 1, 1 |
| Hor. Damping partition | 2.0459 | 1.648 |
| Momentum compaction | $2.798 \times 10^{-2}$ | 0.1408 |
| Energy spread ( $\sigma_{\delta}$ ) <br> @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{gathered} 0.019 \times 10^{-3} / \\ 0.389 \times 10^{-3} \end{gathered}$ | $\begin{gathered} \hline 0.014 \times 10^{-3} / \\ 0.285 \times 10^{-3} \end{gathered}$ |
| Energy loss per turn (keV) @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{gathered} 0.0 / \\ 1.4 \end{gathered}$ | $\begin{gathered} 0.0 / \\ 1.5 \end{gathered}$ |
| Main RF voltage (keV) | 70 | 70 |
| Damping time ( $\mathrm{H} / \mathrm{V} / \mathrm{Z}$ ) (ms) <br> @ $20 \mathrm{MeV} / 400 \mathrm{MeV}$ | $\begin{aligned} & 166066 / 339759 / 356113 \\ & 20.76 \text { / } 42.47 \text { / } 44.51 \end{aligned}$ | $\begin{gathered} 450494 \text { / } 499538 \text { / } 264147 \\ 56.31 / 62.44 \text { / } 33.02 \end{gathered}$ |

Magnet specifications

## Current design

| Type | EA | Length | Max. strength |
| :--- | :---: | :---: | :---: |
| Bend (combined functi <br> on of bend-quad-sext) | 12 | 0.85 m | B0 $=0.822[\mathrm{~T}]$ <br> K1 $=-3.448\left[1 / m^{-2}\right]$ <br> K2 $=-21.576\left[1 / m^{-3}\right]$ |
| 16 cm quad | 14 | 0.16 m | K1 $=20.30\left[1 / \mathrm{m}^{-2}\right]$ |
| 6 cm quad | 8 | 0.06 m | K1 $=4.52\left[1 / \mathrm{m}^{-2}\right]$ |
| Sext | 16 | 0.04 m | K2 $=1116.4\left[1 / \mathrm{m}^{-3}\right]$ |

## Alternative design

| Type | EA | Length | Max. strength |
| :--- | :---: | :---: | :---: |
| Bend (combined functi <br> on of bend-quad) | 12 | 0.80 m | B0 $=0.874[\mathrm{~T}]$ <br> K1 $=-0.260\left[1 / m^{-2}\right]$ |
| 16 cm quad* $^{*}$ | 18 | 0.16 m | K1 $=3.70\left[1 / \mathrm{m}^{-2}\right]$ |
| Sext $^{*}$ | 12 | 0.04 m | K2 $=-36.9\left[1 / \mathrm{m}^{-3}\right]$ |

*reusable

## Comparison on dynamic aperture



Random errors on magnet misalignment (rms value, 2-sigma cut used): 30 um in H/V, 250 um in L


Random errors on magnet misalignment (rms value, 2-sigma cut used):
300 um in H/V, 2500 um in L

* turn = 4096, rf on, sr on, no physical aperture used
* Correction (i.g., orbit correction, LOCO) is not applied for each seed
* 100 error seeds
* The new design rarely reduces for the error which means it is much robust for the error.
* For original lattice, only 3 error seeds have a stable dynamic aperture, for new lattice, all 100 error seeds have it.


## Comparison on momentum aperture




| Ideal lattice | Touschek Lifetime $[\mathrm{h}]$ |
| :---: | :---: |
| Original | 0.11 |
| New | 20916.56 |

* Turn = 8192, rf on, sr on, no physical aperture used
* Charge = 10 pC , Rf voltage = 70 KeV , rf frequency ~ 500 MHz , coupling = 10\%,

IBS effect not considered.

* Ideal local momentum acceptance is much bigger for new design than that of original design.
* Large local momentum acceptance results in long Touschek lifetime for the new design case.
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## PAL-EUV SR parameters



| Parameters | Value |
| :--- | :---: |
| Energy (MeV) | $\mathbf{4 0 0}$ |
| Circumference (m) | $\mathbf{3 6 . 0}$ |
| Emittance (nm) | $\mathbf{1 . 1 8}$ |
| Tunes (H,V) | $\mathbf{7 . 1 5 , 3 . 1 4}$ |
| Natural chromaticity (H,V) | $\mathbf{- 1 0 . 7 , - 1 6 . 9}$ |
| Chromaticity (corrected) <br> (H,V) | $\mathbf{1 , 1}$ |
| Hor. Damping partition | $\mathbf{1 . 8 6}$ |
| Momentum compaction | $\mathbf{1 . 0 3 6 \times 1 0 ^ { - 2 }}$ |
| Energy spread ( $\sigma_{\delta}$ ) | $\mathbf{0 . 3 8 9 \times 1 0 ^ { - 3 }}$ |
| Energy loss per turn (keV) | $\mathbf{1 . 7}$ |
| Damping time (H/V/Z) (ms) | $\mathbf{3 1 . 1 4 ~ / ~ 5 8 . 0 7 ~ / ~ 5 1 . 1 5 ~}$ |
| Beam current (mA) | $\mathbf{1 4 0}$ |

## PAL-EUV SR alternative design-1 (preliminary)



4-bend achromat

## PAL-EUV SR alternative design-2 (preliminary)



## Double-bend achromat

Lattice parameters

| Parameters | Current design (5BA) | Alternative design-1 (4BA) | Alternative design-2 (DBA) |
| :---: | :---: | :---: | :---: |
| Energy (MeV) | 400 | 400 | 400 |
| Circumference (m) | 36.0 | 36.0 | 36.0 |
| Emittance ( nm ) | 1.18 | 3.51 | 11.10 |
| Tunes ( $\mathrm{H}, \mathrm{V}$ ) | 7.15, 3.14 | 6.22 / 3.34 | 3.86 / 2.73 |
| Natural chromaticity ( $\mathrm{H}, \mathrm{V}$ ) | -10.7, -16.9 | -7.2, -8.4 | -7.7, -5.6 |
| Chromaticity (corrected) $(\mathrm{H}, \mathrm{~V})$ | 1,1 | 1, 1 | 1,1 |
| Hor. Damping partition | 1.86 | 1.696 | 1.29 |
| Momentum compaction | $1.036 \times 10^{-2}$ | $1.1 \times 10^{-2}$ | $2.294 \times 10^{-2}$ |
| Energy spread ( $\sigma_{\delta}$ ) | $0.389 \times 10^{-3}$ | $0.467 \times 10^{-3}$ | $0.314 \times 10^{-3}$ |
| Energy loss per turn (keV) | 1.7 | 3.0 | 1.8 |
| Damping time ( $\mathrm{H} / \mathrm{V} / \mathrm{Z}$ ) (ms) | 31.14 / 58.07 / 51.15 | 20.40 / 32.41 / 22.97 | 47.76 / 54.02 / 28.90 |

## Magnet specifications

-Normalized strengths are in MAD unit

| Type | EA | Length | Max. strength |
| :--- | :---: | :---: | :---: |
| Bend (combined functi <br> on of bend-quad) | 20 | 0.43 m | B0 $=0.974[\mathrm{~T}]$ <br> K1 $=-5.59\left[1 / m^{-2}\right]$ |
| 10 cm quad | 56 | 0.10 m | K1 $=23.74\left[1 / \mathrm{m}^{-2}\right]$ |
| Sext | 64 | 0.05 m | K2 $=1818.81\left[1 / \mathrm{m}^{-3}\right]$ |

## Alternative design-1 (4BA)

| Type | EA | Length | Max. strength |
| :---: | :---: | :---: | :---: |
| 40 cm bend (combined function of bend-quad) | 8 | 0.40 m | $\begin{gathered} \mathrm{B} 0=1.747[\mathrm{~T}] \\ \mathrm{K} 1=-7\left[1 / \mathrm{m}^{-2}\right] \end{gathered}$ |
| 20 cm bend <br> (combined function of bend-quad) | 8 | 0.20 m | $\begin{gathered} \mathrm{BO}=1.747[\mathrm{~T}] \\ \mathrm{K} 1=-6.39\left[1 / \mathrm{m}^{-2}\right] \end{gathered}$ |
| 10 cm quad* | 24 | 0.10 m | $\mathrm{K} 1=23.68\left[1 / m^{-2}\right]$ |
| 15 cm quad | 24 | 0.15 m | $\mathrm{K} 1=15.37$ [ $1 / \mathrm{m}^{-2}$ ] |
| Sext* | 52 | 0.05 m | $\mathrm{K} 2=1730.3\left[1 / \mathrm{m}^{-3}\right]$ |

Alternative design-2 (DBA)

| Type | EA | Length | Max. strength |
| :--- | :---: | :---: | :---: |
| Bend (combined <br> function of bend-quad) | 8 | 1.0 m | $\mathrm{B0}=1.047[\mathrm{~T}]$ <br> $\mathrm{K} 1=-0.7\left[1 / \mathrm{m}^{-2}\right]$ |
| 10 cm quad* | 32 | 0.10 m | K1 $=18.20\left[1 / \mathrm{m}^{-2}\right]$ |
| Sext* | 32 | 0.05 m | K2 $=711.0\left[1 / \mathrm{m}^{-3}\right]$ |

[^0]

Random errors on magnet misalignment (rms value, 2-sigma cut used):
30 um in H/V , 250 um in L

## Alternative design-1

 (4BA)

Random errors on magnet misalignment (rms value, 2-sigma cut used):
30 um in H/V, 250 um in L

* rf on, sr on, no physical aperture used
* 100 error seeds, turn = 4096
* Correction (i.g., orbit correction, LOCO) is not applied for each seed
* The new design rarely reduces for the error which means it is much robust for the error.
* For original lattice, only $\mathbf{2 4}$ error seeds have a stable dynamic aperture, for new lattice, all $\mathbf{1 0 0}$ error seeds have it.



## Alternative design-1



| Ideal lattice | Touschek Lifetime $[\mathrm{h}]$ |
| :---: | :---: |
| Original | 26.49 |
| New | 1122.01 |

* Turn = 1024, rf on, sr on, no physical aperture used
* Charge $=10 \mathrm{pC}$, Rf voltage $=70 \mathrm{KeV}$, rf frequency $\sim 500 \mathrm{MHz}$, coupling $=10 \%$,

IBS effect not considered.

* Ideal local momentum acceptance is much bigger for new design than that of original design.
* Large local momentum acceptance results in long Touschek lifetime for the new design case.


## Dipole edge-focusing and tune change

- Including dipole edge-focusing result in tune change in vertical plane
- For a sector bend magnet (pole-face rotation angle $=0$ ), edge focusing at each pole-face is described by a matrix $R$

$$
R=\left(\begin{array}{cccccc}
1 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 0 \\
0 & 0 & \frac{\tan (\psi)}{\rho} & 1 & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & 0 \\
0 & 0 & 0 & 0 & 0 & 1
\end{array}\right)
$$

where $\psi=\kappa_{1}\left(\frac{g}{\rho}\right)$
$\rho=$ Bending radius of central trajectory
$g=$ Total gap of magnet
$\kappa_{1}=A n$ integral related to the extent of the fringing field of a bending magnet
-Current storage ring design has $\rho=1.3698 \mathrm{~m}, g=0.024 \mathrm{~m}$ and $\kappa_{1}=0.5$
-Including dipole edge-focusing changes tune from $\left(v_{x}, v_{y}\right)=(7.152,3.143)$ to $\left(v_{x}, v_{y}\right)=(7.152,3.005)$



Tune adjustment is required after including effect of dipole edgefocusing, in order to restore dynamic aperture

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2D geometry
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PAL-EUV booster

$C=22.2 \mathrm{~m}$

$\mathrm{C}=36.0 \mathrm{~m}$


$$
\mathrm{C}=34.68 \mathrm{~m}
$$


$\mathrm{C}=36.0 \mathrm{~m}$

$\mathrm{C}=36.0 \mathrm{~m}$

## Summary

- Beam Dynamics study on current PAL-EUV lattice design and alternative designs are performed
- Still working on finding an alternative design which keeps current lattice arrangement
- Presented alternative designs aim for relaxed nonlinear properties and robustness against alignment/roll/field errors
- Magnet reusability is also considered
- Alternative design on booster is much more robust against errors, but it doesn’t fit current 22.2 m geometry
- Alternative design-1 on storage ring can provide similar dynamic aperture to that of current design but can provide much longer Touschek lifetime


## Thank you for your attention



PAL POHANG accelerator labooatory


[^0]:    *reusable

